

Supplementary file for:

# Small signal stability analysis of a four machine system with placement of multi-terminal high voltage direct current link

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Table 1: Multiterminal high voltage direct current data.

Parameter	Rect-1	Rect-2	Invtr
Rated/Actual power (MW)	300/198	1000/460	1200/700
Rated/Actual DC current (kA)	0.3/0.2	1.0/0.5	1.2/0.75
$\alpha$ for rectifier, $\gamma_0$ for inverter	14.8	18	15
<b>Transformer per 6 pulse thyristor</b>			
Rating (MVA)	350	1000	1200
Voltage (kV)	230/500	230/500	500/230
Leakage reactance (pu)	0.18	0.18	0.18
<b>PI controller</b>			
Proportional gain	1.0989	1.5363	1.5363
Integral time constant (s)	0.01092	0.01524	0.01524
<b>VDCOL</b>			
Threshold input	0.4-1.0	0.4-0.9	0.4-0.9
Threshold output	0.55-1.5	0.55-1.0	0.55-1.0

Table 2: Synchronous machine data.

Generator data		AVR and PSS	
$ra$	0.0025 pu	<i>Input signal</i>	Speed
$xl$ or $xp$	0.130 pu	$T_R$	0.01 sec
$xd$	1.81 pu	$V_{imax}$	10 pu
$x'd$	0.3 pu	$V_{imin}$	-10 pu
$x''d$	0.25 pu	$K_A$	200 pu
$T'd0$	8.0 sec	$Efmax$	7.0 pu
$T''d0$	0.03 (s)	$Efmin$	-6.4 pu
$xq$	1.7 pu	$K_{STAB}$	20
$x'q$	0.55 pu	$T_W$	10 sec
$x''q_0$	0.25 pu	$T_1$	0.05 sec
$T'q0$	0.4 (s)	$T_2$	0.02 sec
$T''q_0$	0.03 (s)	$V_{stmax}$	0.2
$H$	6.5 A1, 6.177 A2	$V_{stmin}$	-0.2

Table 3: Transmission line data

<b>DC Transmission line (T-model) data</b>	
R( $\Omega/\text{km}$ )	0.01
Reactor (H)	0.5968
DC filter ( $\mu\text{F}$ )	15
<b>AC Transmission line data</b>	
r (pu/km)	1e-4
x <sub>L</sub> (pu/km)	1e-3
b <sub>c</sub> (pu/km)	1.75e-3

### Nomenclature

$H$	Inertia constant in s
$K_D$	Machine load damping coefficient
$ra$	Armature resistance in p.u
$xd$	Unsaturated d axis synchronous reactance in p.u
$xq$	Unsaturated q axis synchronous reactance in p.u
$x'd$	Unsaturated d axis transient reactance in p.u
$x'q$	Unsaturated q axis transient reactance in p.u
$x''d$	Unsaturated d axis sub transient reactance in p.u
$x''q$	Unsaturated q axis sub transient reactance in p.u
$xl$ or $xp$	Leakage or Potier reactance in p.u
$T'd0$	d axis transient open-circuit time constant in s
$T''d0$	d axis sub transient open-circuit time constant in s
$T'q0$	q axis transient open-circuit time constant in s
$T''q0$	q axis sub transient open-circuit time constant in s
$Te$	Exciter time constant in s
$P_{max}$	Maximum turbine output in p.u
$K_{STAB}$	Stabilising gain,
$T_1$	First lead time constant,
$T_2$	First lag time constant,
$T_w$	Washout time constant,
$K_A$	Regulator integral gain,
$T_R$	Transducer time constant,
$\Delta\omega_r$	Change in angular speed,
$E_{fd}$	Exciter output voltage,
$V_{stmax}, V_{stmin}$	Minimum and maximum regulator outputs,

$V_{ref}$	Reference voltage regulator,
$V_s$	Combined power system stabiliser and possibly discontinuous control output after any limits or switching,
$E_t$	Terminal voltage of transducer and load compensation elements
$R$	Direct current line resistance in $\Omega/\text{km}$
$r$	Alternating current line resistance in $\text{pu}/\text{km}$
$x_L$	Alternating current line reactance in $\text{pu}/\text{km}$
$b_c$	Alternating current line capacitive impedance in $\text{pu}/\text{km}$
$\text{pu}$	Per unit
PI	Proportional and integral
Rect-1	Rectifier 2
Rect-2	Rectifier 1
Invtr	Inverter
VDCOL	Voltage dependent current order limiter
PSS	Power system stabiliser
AVR	Automatic voltage regulator
AC	Alternating current
DC	Direct current
$\alpha$	Firing angle for rectifier
$\gamma_0$	Initial extinction angle for inverter
MW	Active power in mega watt
MVA	Apparent power in mega volt amperea
KV	Kilo-volt
KA	Kilo-ampere
s	Second