

Cluster analysis for classification and forecasting of solar irradiance in Durban, South Africa

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Abstract

Clustering of solar irradiance patterns was used in conjunction with cloud cover forecasts from Numerical Weather Predictions for day-ahead forecasting of irradiance. Beam irradiance as a function of time during daylight was recorded over a one-year period in Durban, to which k-means clustering was applied to produce four classes of day with diurnal patterns characterised as sunny all day, cloudy all day, sunny morning-cloudy afternoon, and cloudy morning-sunny afternoon. Two forecasting methods were investigated. The first used k-means clustering on predicted daily cloud cover profiles. The second used a rule whereby predicted cloud cover profiles were classified according to whether their average in the morning and afternoon were above or below 50%. In both methods, four classes were found, which had diurnal patterns associated with the irradiance classes that were used to forecast the irradiance class for

the day ahead. The two methods had a comparable success rate of about 65%; the cloud cover clustering method was better for sunny and cloudy days; and the 50% rule was better for mixed cloud conditions.

Keywords: numerical weather prediction; cloud cover; k-means; classes

Highlights:

- Clustering produced four classes of beam irradiance profiles for Durban
- Numerical weather prediction cloud cover patterns into four classes
- Association of classes used for day-ahead forecasting of beam irradiance
- Forecasting had a moderate success rate of about 65%

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Nomenclature

Abbreviations

NWP	numerical weather prediction	ANN	artificial neural network
SUI	solar utility index	TOA	top of atmosphere
GHI	global horizontal irradiance	SAST	South African standard time
DHI	diffuse horizontal irradiance	PCA	principal component analysis
DNI	direct normal irradiance	RMSE	root mean square error
NOAA	National Oceanic and Atmospheric Administration		

Symbols

k_t	clearness index	T_L	Linke turbidity coefficient
k_b	direct horizontal irradiance fraction	C	cloud cover percentage
B	beam irradiance	SI	silhouette index
B_n	normalised beam irradiance	$\bar{S}I_C$	average silhouette index for an individual cluster
B_c	Ineichen model clear sky beam component	$\bar{S}I_{TOT}$	average silhouette index for the entire set of objects in a cluster
\bar{B}_n	hourly average of the normalised beam irradiance	C_{AM}	morning cloud cover average
n	number of minutes	C_{PM}	afternoon cloud cover average
i	minute index		

1. Introduction

Characterisation and forecasting of solar irradiation patterns has become increasingly important for designing, operating and managing grid-connected solar power plants. Knowledge of typical solar irradiance at a given location, and how it varies from day to day, allows power plant operators to estimate power output. It is also useful for forecasting power output because knowledge of common irradiance patterns may be used to constrain a forecast to fall with a high probability into one of those patterns.

An approach to understand solar resource patterns includes classification and characterisation of irradiance profiles by cluster analysis, where a profile is defined as irradiance and a function of time over a day. Classification is useful for forecasting because, if the class of a day can be successfully forecast, the irradiance profile of that day would share the general pattern of the class. Forecasting employs a range of techniques, including using NWP and satellite imagery of cloud cover to predict how cloud cover changes over space and time (Inman et al., 2013). Several studies (Mathiesen et al., 2013; Lorenz et al., 2009; Remund et al., 2008; Perez et al., 2007; Aguiar et al., 2016) successfully employed

NWP models together with other techniques for solar forecasts.

Other studies (Muselli et al., 2000; Maafi and Harrouni, 2003; Diabaté et al., 2004; Harrouni et al., 2005; Soubdhan et al., 2009; Gastón-Romeo et al., 2011 and Zhandire, 2017) investigated classification of days based on solar irradiance but did not consider forecasting. The irradiance characteristics of Durban, KwaZulu-Natal Province, South Africa, which has a humid sub-tropical climate and significant cloud variation, has been described by Lysko (2006), Zawilska and Brooks (2011) and Kunene et al. (2013), but not using clustering of irradiance profiles. Clustering was used by Zhandire (2017) to produce classes of a SUI for each of nine stations across South Africa. The SUI was a daily average of beam and diffuse horizontal irradiance. Zhandire did not consider beam irradiance independently or the diurnal variation of beam irradiance. In addition, the primary aim of that study was to provide a new solar resource index for classification for multiple stations across South Africa, and did not aim exclusively to characterise the solar irradiance patterns in Durban or investigate the possibility of forecasting using classification results.

The most commonly-used classification variable is k_t , which is the ratio of the measured GHI to the TOA irradiance. Studies that use classification for forecasting include those by McCandless et al. (2014, 2015), where identification of different cloud regimes, subsequently solar irradiance forecasting models: ANNs, were built specifically to predict k_t for each regime. McCandless et al. (2014) tested forecasts up to three hours ahead, and McCandless et al. (2015) used k -means clustering to identify seven cloud regimes based on the previous 45 minutes of k_t for a 15-minute forecast. McCandless et al. (2014) identified cloud regimes by k -means clustering but tested forecasts up to three hours ahead rather than day forecasts. Furthermore, McCandless et al. (2015) merely considered the use of NWP for forecasting without applying it.

Badosa et al. (2013) presented a characterisation of mesoscale and local-scale solar irradiance variability for Reunion Island, which showed that the island's diurnal irradiance variation can be classified into five classes. Badosa et al. (2015) explored the variability in local irradiance conditions and cloud cover dynamics of Reunion Island using irradiance classes defined in Badosa et al. (2013) together with synoptic wind and relative humidity parameters. Jeanty et al. (2013) investigated irradiance patterns for Reunion Island using cluster analysis applied to daily profiles of direct horizontal irradiance fraction, k_b , defined as $1 - \text{DHI}/\text{GHI}$, where DHI is diffuse horizontal irradiance. Similar to Badosa et al. (2013), the study revealed five dominant patterns for the island. However, only four of the five patterns, corresponding to clear, cloudy, AM clear and PM clear conditions, are positively correlated with the classes obtained by Badosa et al. (2013).

Badosa et al. (2013; 2015) and Jeanty et al. (2013) served as a basis for much of the present study, where minute-resolution irradiance profiles similar to those of Jeanty et al. were pre-processed by PCA and then clustered by the k -means method. This method produced a set of classes of differing diurnal variation that characterise the irradiance patterns in Durban. Clustering was also applied to hourly-averaged beam irradiance, and the classes obtained were compared with those obtained from the minute-resolution data. Although knowledge of both beam and global irradiance is important for solar power plants, the present investigation was restricted to beam irradiance to test a method suitable for extension to forecasting of global irradiance. Presented here is an approach that applies clustering to both radiometric data and NWP cloud cover for day-ahead forecasting of direct (beam) irradiance, which is tested against a simple decision rule using morning and afternoon averages of cloud cover. The NWP provides day-ahead cloud cover forecasts with an hourly temporal resolution, and cloud cover

is used here for forecasting because of its strong association with beam irradiance intensity.

The forecasting model starts with an NWP day-ahead forecast of hourly cloud cover percentage and uses it to predict the irradiance class for that day. This is compared with the day's actual irradiance class, and the predicted irradiance profile is the mean profile of the class, which is compared with the actual irradiance profile of the day. In Section 2, the radiometric data used for this study is described and the variables used for clustering and forecasting are defined. The section also includes a motivation for the choice of the beam irradiance component for clustering and forecasting. Thereafter details of the clustering and forecasting methods are described. In Section 3, results of the clustering of radiometric and cloud cover data are given. Forecasting results are also presented, including a comparison of the performance of the two forecasting methods. A discussion of the clustering and forecasting results is presented in Section 4. Conclusions of the main findings are given in Section 5.

2. Method

2.1 Data and definition of variables

Irradiance data were collected at the University of KwaZulu-Natal, Durban, South Africa (29.87° S; 30.98° E). The radiometric station, which is part of the SAURAN network (Brooks et al., 2015), is located 150 m above mean sea level, on a roof platform. Measurements for DNI were obtained using a Kipp & Zonen CHP1 pyrheliometer. The instrument was mounted on a Solys2 automatic sun tracker. Measurements were taken every two seconds and averaged over one-minute intervals. Daily profiles of DNI were recorded at one-minute intervals from 8:30 to 16:30 solar time. This restricted time interval was chosen to avoid sensor shading during early morning and late afternoon in winter. The radiometric data were manually checked for quality and to identify anomalies. This was coupled with a forecast of hourly C obtained from AccuWeather, a public weather service provider, to produce a daily profile from 9:00 to 16:00 SAST. The output was derived from an NWP model run by the NOAA.

The irradiance measurements were used to define minute-resolution and hourly-resolution profiles for clustering. Let B denote beam irradiance (DNI) at one-minute resolution, where B_n is defined as B normalised to the beam component B_c of the Ineichen clear sky model (Ineichen and Perez, 2002) for Durban as expressed by Equation 1.

$$B_n = \frac{B}{B_c} \quad (1)$$

Then, let \bar{B}_n denote the hourly average of B_n to produce Equation 2.

$$\bar{B}_n = \frac{1}{n} \sum_{i=1}^n B_{ni} \quad (2)$$

where i is the minute index and $n = 60$. The first minute ($i = 1$) is on the half-hour, e.g. 9:30, values of \bar{B}_n are known at times 9:00, 10:00, 11:00, ... 16:00.

The normalised beam irradiance, B_n , is used rather than beam fraction k_b , because it removes seasonality. Near dawn and dusk, DNI is close to zero, and DHI is almost equal to GHI, therefore, $k_b \approx 0$. On a clear day, k_b rises in the first hour after dawn to near unity and declines in late afternoon during the last hour before sunset. As the seasons change, sunrise and sunset times change, causing the k_b profiles to vary in the start and end times of the rising and declining phases. This seasonal variation in profile, even for clear days, creates differences that are not produced by cloud conditions. Given that a primary objective was to cluster profiles in accordance with how they are affected by clouds, B_n was chosen rather than k_b because the shape of the B_n profile is independent of seasonality. The B_n is zero before sunrise and after sunset and these times vary with season; and between these times its shape depends on cloud conditions, but for a clear day, its profile is a horizontal line. Figure 1 shows k_b for B_c , the clear-sky beam, for the winter and summer solstices, where $k_b = 1 - D_c/G_c$, and the Ineichen clear sky model diffuse and global irradiance are D_c and G_c , respectively.

The Ineichen model is preferred over other clear sky models since the only atmospheric parameter required is the Linke turbidity coefficient T_L for the lo-

cation. Monthly averages of the T_L values for Durban were estimated using local radiometric data with the MATLAB implementation of the clear sky model developed by Sandia National Laboratories (SNL, 2012).

2.2 Clustering

For data with high dimensionality, in this case B_n , PCA was performed prior to clustering as a pre-processing step. The method was implemented in MATLAB (R2015a) using the Statistics Toolbox. The PCA reduces the dimensionality of a data set, while preserving most of the variance in the data. As described by Jolliffe (2002), this is achieved by transforming to a new set of axes, called principal components, which are ordered successively so that the first few components retain most of the variation present in the original data. The cumulative percentage of the total variation was used to choose the minimum number of principal components to be retained, where the minimum number of components with a cumulative percentage of 90% was retained.

To obtain classes of pre-processed B_n , and of \bar{B}_n and C , k -means clustering was applied, also implemented in MATLAB. The k -means algorithm, developed by MacQueen (1967) is a well-known and commonly-used partitioning clustering algorithm (Halkidi, 2001). It partitions a set of n objects into k clusters, where the number of clusters, k , is specified in advance. In this case, each object is a daily profile of one of the variables defined above. The profile may be represented by a position in a multi-dimensional space on which a metric is defined to calculate

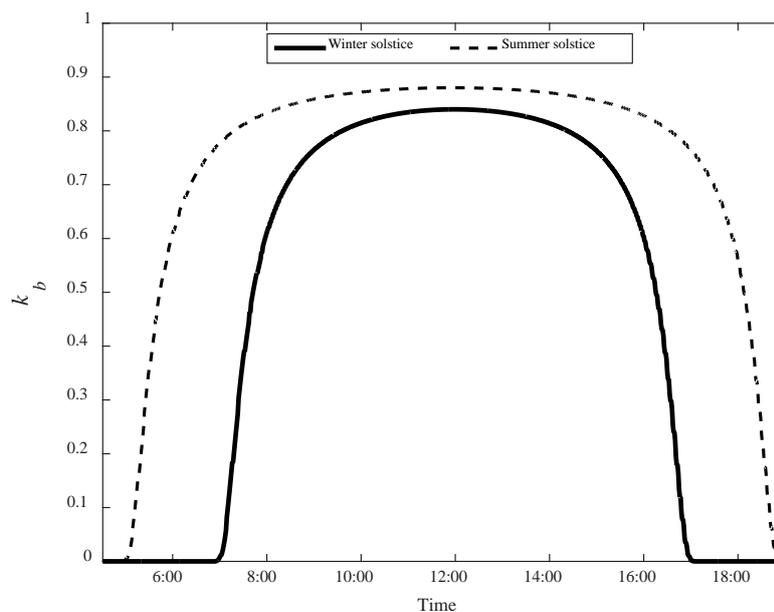


Figure 1. The direct horizontal irradiance profiles derived from the Ineichen clear sky model at winter and summer solstices in Durban.

the distance between positions. According to Rousseeuw (1957), the compactness and separation of clusters is quantified by the SI, which varies from -1 to 1 , where an SI that approaches 1 is indicative of an object being ‘well-clustered’. On the other hand, SI approaching -1 indicates that the object is not well-suited to that cluster (Zagouras et al., 2014; Rousseeuw, 1957). The average SI for an individual $\bar{S}I_C$, where C is a cluster label, or for the entire set of objects (denoted here as $\bar{S}I_{TOT}$) is used as an index of overall clustering compactness. Lletí et al. (2004) consider a silhouette value of 0.6 or greater to be a good clustering result, which will be used here as a criterion for acceptable compactness. The number of clusters was not determined by a specific criterion, but by consideration of the results for various values of k , guided by $\bar{S}I_{TOT}$ as well as values of $\bar{S}I_C$ for each cluster. The aim of the present study was to find the ‘natural’ clustering, which corresponds with finding the largest number k of compact clusters. The guideline used was to maximise k , while keeping $\bar{S}I_{TOT}$ greater than 0.6 and seeking to maintain $\bar{S}I_C$ as high as possible for each of the clusters obtained. Classification of daily profiles was based on the clusters that were determined, the terms ‘cluster’ and ‘class’ are used interchangeably.

2.3 Forecasting

Let the class mean profile (\bar{B}_n) denote the mean of the set of B_n profiles for a class. Forecasting was done by using a day-ahead forecast of C to forecast the class of the day and then using \bar{B}_n for that class as the forecast of the B_n profile. Although C was specified on the hour in ‘clock time’ (SAST), and hence offset from solar time, the difference of at most 20 minutes was small compared with the one-hour resolution of the C profile and was not significant. Forecasting was done using two methods. The first uses classes of C found by k -means clustering. The forecast of C is assigned to one of the classes, which in turn is associated with one of the classes of \bar{B}_n . The second method, the ‘50% rule’, uses a set of decision rules based on C . Both methods depend on the clustering results and these are described further in Section 3. The profiles forecast using both methods are compared with the actual B_n for the day by computing the RMSE given by Equation 3.

$$RMSE = \sqrt{\frac{\sum_{i=1}^n (\bar{B}_{n_actual_i} - \bar{B}_{n_forecast_i})^2}{n}} \quad (3)$$

where $\bar{B}_{n_actual_i}$ and $\bar{B}_{n_forecast_i}$ are the actual and forecast profiles, respectively, and n is the number of hours in the time interval. The actual profile is that derived from radiometric measurements, whereas the forecast profile is the mean profile of the class that is forecast.

3. Results

3.1 Data

For clustering of radiometric data to establish classes, the set contained 365 days from 28 January 2014 to 27 January 2015 . Clustering of cloud cover (from NWP forecasts) was applied to a set of 243 days in 2016 , approximately uniformly distributed throughout the year, where missing days were almost all weekends. There was no requirement that the radiometric data and NWP cloud cover be in the same year because clustering was applied to find patterns that were independent of a specific year. Testing of forecasting was done using a set of 100 days in 2017 , including most days during the months of January to June.

3.2 Clustering of minute-resolution normalised beam irradiance

Each daily profile of B_n consisted of a set of 481 values for each minute during the interval $8:30$ to $16:30$ solar time. Therefore, each B_n profile corresponded to a point in a 481 -d space, which was reduced to a low-dimensional space by PCA. The first eight components accounted for 90% of the variance and were hence retained.

The clustering results for the daily profiles of B_n in 8 -d space were almost identical to those for \bar{B}_n , producing identical classes with identical members, consequently only the results of clustering of \bar{B}_n are presented. This high degree of similarity indicates that the sub-hourly temporal structure in B_n did not result in any significant difference in clustering compared with the temporal structure in the hourly average.

3.3 Clustering of hourly-resolution normalised beam irradiance

The daily profiles of \bar{B}_n were clustered using k -means for $k = 4$, since $\bar{S}I_{TOT} = 0.65$ was found to be the highest for 4 clusters. This was selected as the final clustering result. Clusters A and B have $\bar{S}I_C$ of 0.79 , and clusters C and D have $\bar{S}I_3 = 0.33$ and $\bar{S}I_4 = 0.25$. Table 1 summarises the clustering information.

Table 1. Hourly-resolution normalised beam irradiance clustering information for $k = 4$ solution.

Class	$\bar{S}I_C$	$\bar{S}I_C < 0$	Proportion of days (%)
A	0.79	0	37
B	0.79	0	34
C	0.33	9	18
D	0.25	7	11

The four \bar{B}_n clusters are represented in Figure 2, which shows morning ($8:30$ – $12:30$) average of \bar{B}_n

on the horizontal axis and afternoon (12:30–16:30) average on the vertical axis. Clusters A and B are compact and widely separated, whereas clusters C and D, in the region between A and B, are less compact and have members at their edges that are closer on average to A and B than to their own cluster, resulting in negative SI for those members. A minor difference between the \bar{B}_n and B_n clustering is that the number of profiles with negative SI decreased from 19 for B_n to 16 for \bar{B}_n .

Since beam irradiance is strongly correlated with

cloud cover, Figure 3 shows that there are four classes of diurnal variation in beam irradiance on the half-day scale: sunny all day (cluster A); cloudy all day (cluster B); sunny in the morning and cloudy in the afternoon (cluster C); and cloudy in the morning and sunny in the afternoon (cluster D). These clusters are hence identified as irradiance pattern classes, which are labelled as: Class A: sunny, Class B: cloudy, Class C: sunny AM-cloudy PM, and Class D: cloudy AM-sunny PM. The diurnal patterns shown in Figure 2 are evident in the class mean profiles plotted in Figure 3.

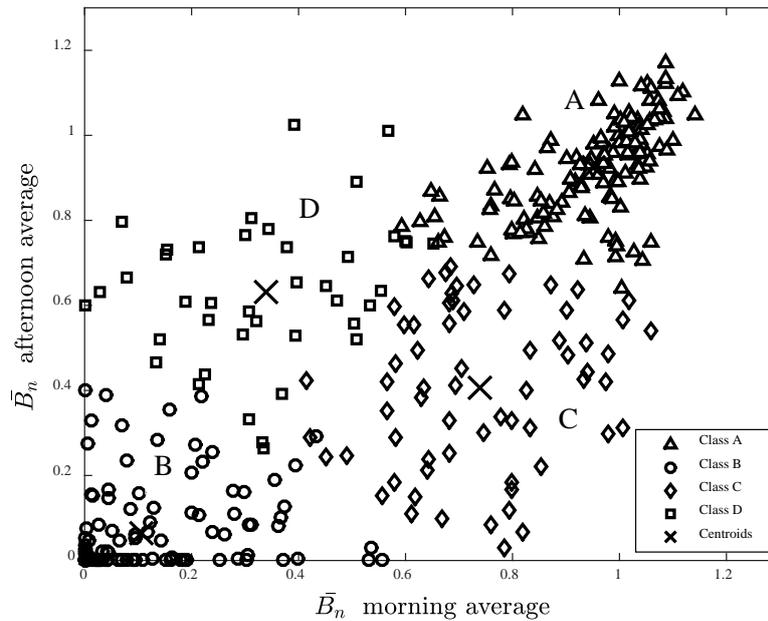


Figure 2. Cluster map of hourly-resolution normalised beam irradiance. Class A days have high morning and afternoon averages, whereas Class B is low for both. Classes C and D have a combination of low and high averages.

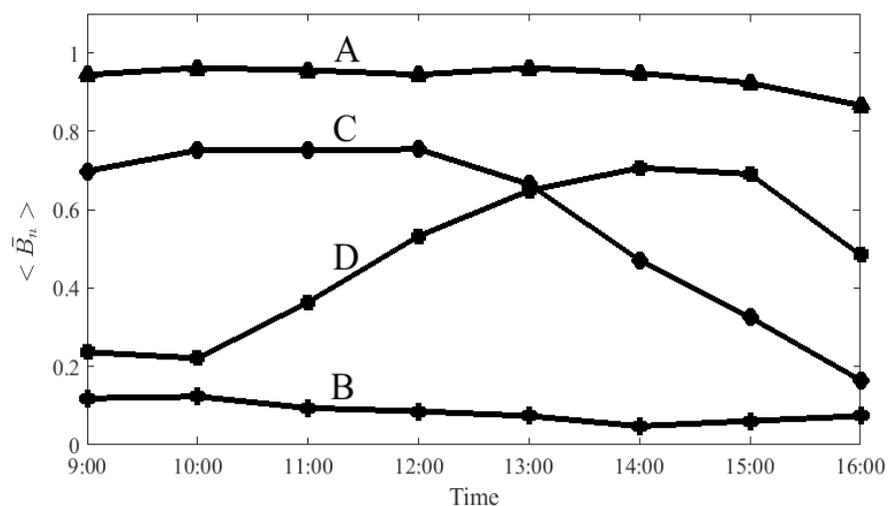


Figure 3. Mean profiles of the hourly-resolution normalised beam irradiance classes. Cloudy (B) and sunny (A) conditions are characterised by low and high beam irradiance values, respectively. The sunny periods of classes C (sunny-cloudy) and D (cloudy-sunny) do not receive the same irradiance levels as Class A. Similarly, the cloudy periods of classes C and D are less cloudy as compared to Class B.

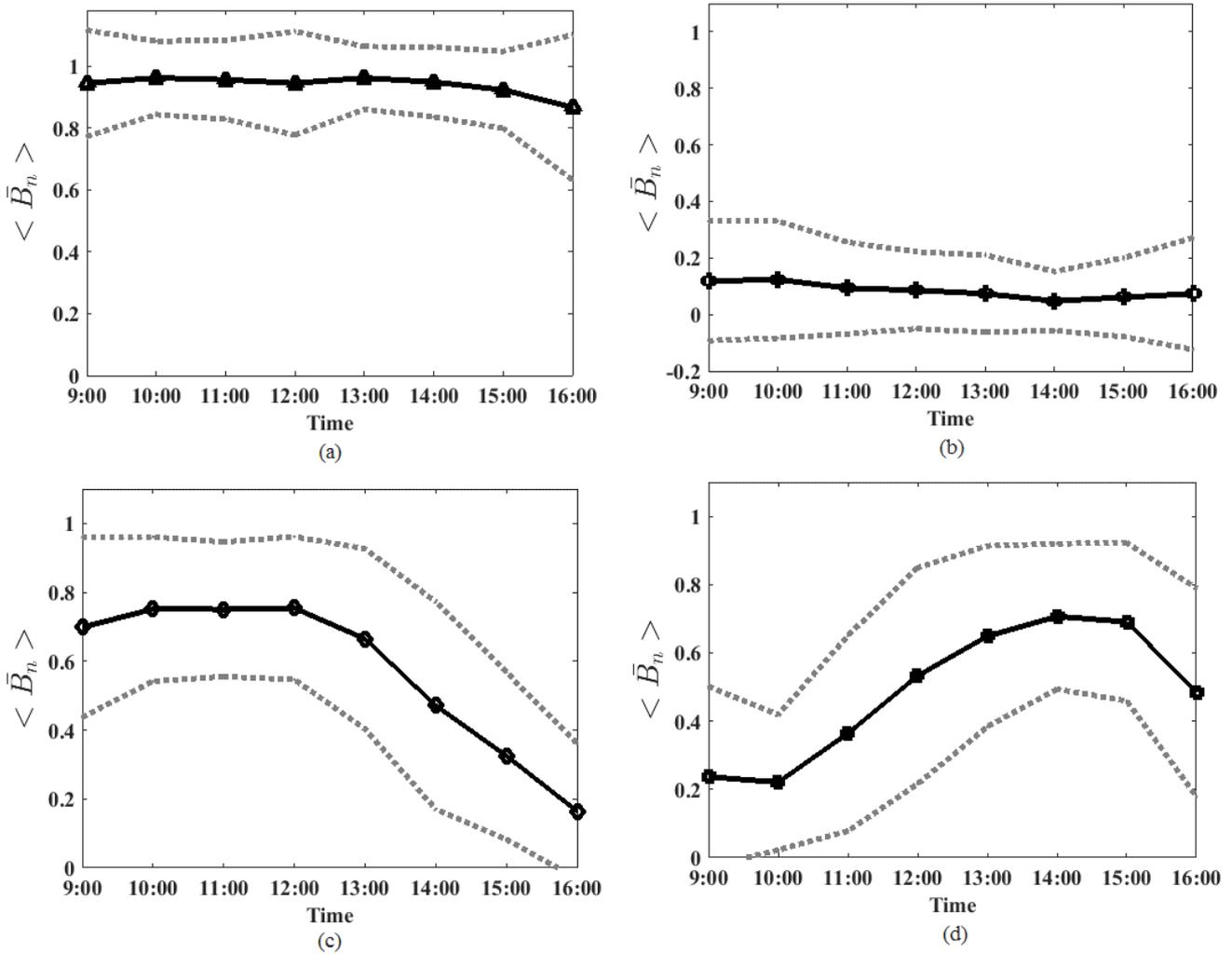


Figure 4. Class mean profiles of hourly-resolution normalised beam irradiance for (a) sunny, (b) cloudy, (c) sunny-cloudy, and (d) cloudy-sunny. Range of uncertainty (dashed line) shown as one standard deviation for each class mean profile (solid line) calculated for each hour.

It is important to have knowledge of the range of uncertainty for forecasting, which is shown in Figure 4(a)–(d) as plots of standard deviation for each class mean profile, calculated for each hour. The more compact clusters, A and B, have lower standard deviation than the less compact clusters, C and D. A forecast that places a day into a class will, therefore, be predicted to have an irradiance profile similar to that class mean profile within an uncertainty corresponding to the class standard deviation. It is, therefore, expected that forecasts of A and B class will have less uncertainty than for C and D.

3.4 Clustering of cloud cover

It was necessary to have four classes of cloud cover in order to use classes of C to forecast the irradiance class. Because low \bar{B}_n is correlated with high C, it was expected that they should exhibit similar clustering, considering that NWP is designed to model the weather pattern as accurately as possible. It was found that $k = 4$ was a good solution, with $\bar{S}I_{TOT} =$

0.74. Table 2 summarises the results of clustering of daily C profiles.

Table 2. Cloud cover clustering information for $k = 4$ solution.

Class	$\bar{S}I_C$	$\bar{S}I_C < 0$	Proportion of days (%)
A'	0.86	0	26
B'	0.88	0	44
C'	0.46	2	8
D'	0.42	4	21

Figure 5 shows a cluster map with morning average of C on the horizontal axis and the afternoon average on the vertical axis. The four clusters have cloud cover conditions that are associated with the \bar{B}_n classes and are given the same labels, but with primes. The C classes are, therefore, Class A': low C all day, Class B': high C all day, Class C': low C in

the morning and high C in the afternoon, and Class D' : high C in the morning and low C in the afternoon.

The diurnal variation in C is shown in Figure 6 as a plot of class mean $\langle C \rangle$ for the four classes.

3.5 Forecasting

As mentioned previously, two approaches were used to apply a cloud cover forecast to determine a \bar{B}_n forecast. The first was to use the four classes of C obtained from clustering. For a given day, the C forecast was obtained; and the day was assigned to one of the C classes by finding the nearest centroid

in the 8-d cluster space. The associated irradiance class was then regarded as the forecast of the irradiance class of that day. The forecast irradiance profile is the class mean profile, with estimated uncertainty given by the class standard deviation. For example, suppose that a given day is forecast to belong to C class A' . Then the irradiance forecast is that the day belongs to the associated \bar{B}_n class A .

The forecasting results using the classes of C are presented in Table 3. Each cell in Table 3 shows the number of days in a predicted class that were found to be in an actual class, with marginals in the right-most column and lowest row. Shown in brackets are

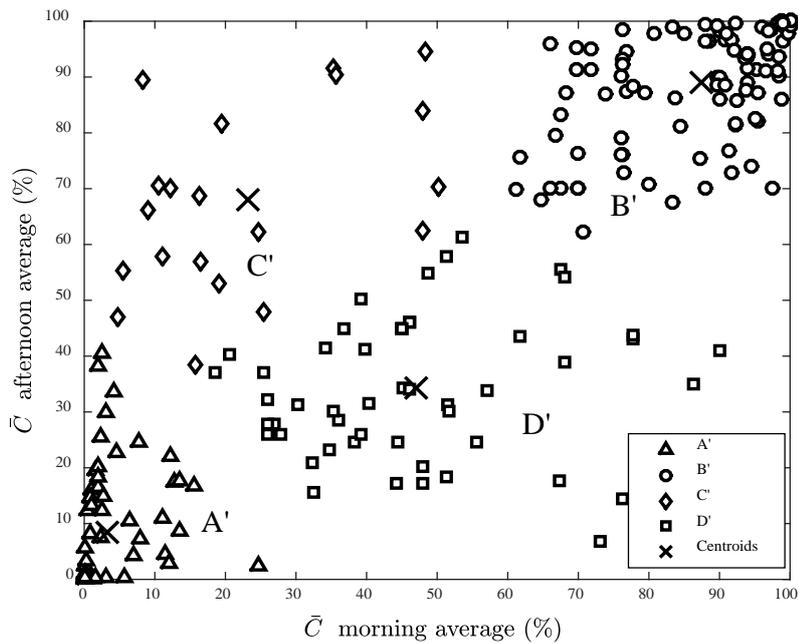


Figure 5. Cluster map of cloud cover with daily profiles averaged for morning and afternoon, where A' , B' , C' , and D' denote sunny, cloudy, sunny mornings and cloudy afternoons, cloudy mornings and sunny afternoons, respectively.

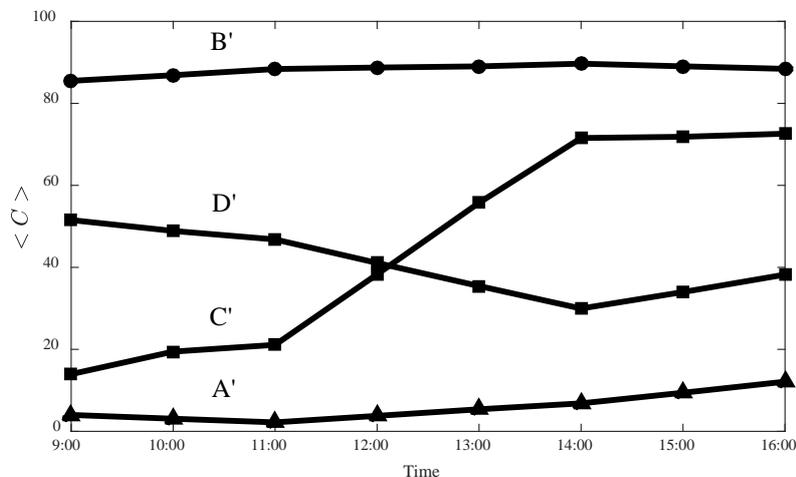


Figure 6. Daily mean profiles of cloud cover. Sunny days (A'), cloudy days (B'), sunny mornings and cloudy afternoons (C'), and cloudy mornings and sunny afternoons (D').

Table 3. Forecast results using clustering of C on the testing sample of 100 days in 2017.

		Actual beam irradiance class				Total forecast
		A	B	C	D	
Predicted beam irradiance class	A	26 (72%)	1 (3%)	4 (11%)	5 (14%)	36
	B	0 (0%)	23 (66%)	8 (23%)	4 (11%)	35
	C	3 (30%)	2 (20%)	5 (50%)	0 (0%)	10
	D*	2 (11%)	4 (21%)	2 (11%)	11 (57%)	19
Total actual		31	30	19	20	100

Note: Each cell shows the number of days in a predicted class that were found to be in an actual class, with marginals in the rightmost column and lowest row. Shown in brackets are the number in a cell as a percentage of the total in the rightmost column.

* The value in row D, column D has been rounded down so that the row adds to 100%.

the number in a cell as a percentage of the total in the rightmost column. For example, the first row shows the 36 days predicted to be in class A, of which 26 were in Class A, 1 in B, 4 in C and 5 in D. Thus 72% of days predicted to be in Class A were in Class A, whereas 3% were actually in Class B, 11% in C and 14% in D. The number of correct predictions is in the main diagonal.

Table 3 shows that prediction success rate per class ranges from 50–72%, with Classes A and B having the highest rates. Regarding incorrect predictions, predicted Class A was actually Class B for only one day (3%) and predicted Class B was actually Class A in zero cases. This is because, for a good NWP, it should be unusual for a sunny day to be wrongly forecast as a cloudy day and vice-versa. Classes C and D had a higher percentage of incorrect predictions, although Class D's success rate of 58% is not much lower than that of Class B. The success rate of 65% over all classes may only be applied to the period January to June from which the sample of 100 days was drawn, but it so happens that a standardised rate based on weighting with class frequencies over one year, given in Table 1, also gives a success rate of 65%.

The second forecasting method uses a simple decision rule, termed the '50% rule' because it assigns a C profile to a class depending on whether the morning average (C_{AM}) and afternoon average (C_{PM}) are above or below 50%. This method was chosen as a simple alternative to clustering that considers the diurnal variation of the \bar{B}_n classes. The 50% rule is described in Table 4.

The forecasting results using the 50% rule are presented in Table 5, which has the same format as that of Table 3.

Table 4. Decision rules for morning and afternoon average cloud cover percentage and the associated hourly-resolution beam irradiance class.

Associated beam irradiance class	(C_{AM} in %)	(C_{PM} in %)
A	≤ 50	≤ 50
B	> 50	> 50
C	≤ 50	> 50
D	> 50	≤ 50

Table 5 shows that the 50% rule produces prediction success rate per class in the range 59–83%, which is somewhat better than that of the C clustering forecast, except that there is a higher rate (9%) of Class B incorrectly predicted as Class A. The Class D success rate is significantly better, although the sample is rather small. Furthermore, Class D predicted by the 50% rule has only about a third of the days predicted to be in Class D by C clustering because, as may be seen in Figure 5, Class D' has a large number of days with $C_{AM} \leq 50\%$, which are therefore predicted by the 50% rule to be in Class A. This increased the number of sunny (Class A) days predicted by the 50% rule. A consequence is that the 50% rule results in more Class A days being incorrectly predicted than in the C clustering method. In comparison with C clustering, the prediction success rate decreased for Classes A and B (by 8% and 7%, respectively) and increased for Classes C and D (by 13% and 25%). The overall raw success rate is 63%, and the standardised success rate is 64%, both of which, apart from being almost identical, are very close to that of the C clustering method.

Table 5. Forecasting results using the 50% rule.

		Actual beam irradiance class				Total forecast
		A	B	C	D	
Predicted beam irradiance class	A	30 (64%)	4 (9%)	4 (9%)	9 (19%)	47
	B	0 (0%)	23 (59%)	10 (26%)	6 (15%)	39
	C	1 (13%)	2 (25%)	5 (63%)	0 (0%)	8
	D	0 (0%)	1 (17%)	0 (0%)	5 (83%)	6
	Total actual	31	30	19	20	100

Note: Each cell shows the number of days in a predicted class that were found to be in an actual class, with marginals in the rightmost column and lowest row. Shown in brackets are the number in a cell as a percentage of the total in the rightmost column.

Table 6 shows the average RMSE values, computed using Equation 3, for each class using the respective forecasting method. Overall, the average RMSE per class are similar using the two forecasting methods, with smaller RMSE for Classes A and B using *C* clustering, and smaller RMSE for Classes C and D using the 50% rule. The largest difference is in Class A.

Table 6. Average RMSE for each class using the two forecasting methods.

Class	50% rule	<i>C</i> clustering
A	0.27	0.20
B	0.24	0.22
C	0.29	0.32
D	0.29	0.34

4. Discussion

Clustering one year of radiometric profiles (\bar{B}_n) yielded four classes that describe diurnal patterns in Durban. It turned out that PCA applied to the 481-dimensional B_n (minute-resolution) profiles resulted in the same clusters obtained from \bar{B}_n (hour-resolution), which indicates that hour-resolution profiles contain sufficient information for the four main clusters. These were very similar to four of the five classes obtained for Reunion Island by Jeanty et al. (2013) and Badosa et al. (2013). They were also similar to the three classes obtained by McCandless et al. (2014), of which the sunny (Class A) and cloudy days (Class B) formed two distinct classes whereas the partly cloudy days in the McCandless et al. (2014) classification were subdivided here by diurnal pattern into Classes C and D.

Two methods were tested to forecast daily beam irradiance profiles from cloud cover output of NWP: *C* clustering and the 50% rule. The forecasting results showed that the two methods produced comparable prediction success rates in the range 50–83%. The overall success rates were about 65% for both methods, with variation for the different classes. The *C* clustering showed the best performance in predicting sunny days (Class A), followed by cloudy days (Class B). This may be due to the NWP model being able to distinguish between cloud-free and cloudy situations relatively well. By contrast, the 50% rule had a success rate that is better for the mixed conditions of Classes C and D. This may be due to the stronger separation of cloud cover conditions by the 50% rule as compared with clustering. Average profile error as quantified by RMSE was in the range 0.2–0.34. These results are similar to those of Badosa et al. (2015), where the lowest RMSE was for sunny conditions. However, in contrast to the present study where the highest RMSE were found for mixed conditions, Badosa et al. (2015) found the highest forecasting errors were associated with cloudy conditions. The main difference in the methods is that the present work used cloud cover output of NWP, with clustering of cloud cover profiles, and uses beam rather than global irradiance.

The novelty of this investigation is the use of clustering of cloud cover output from NWP, as well as the 50% rule, for day-ahead forecasts of beam irradiance using classification of daily irradiance profiles. The forecasting methods have moderate success, which may be attributed both to the degree of accuracy of NWP and the existence of clusters of diurnal irradiance profiles, which show a high degree of clustering for sunny and cloudy conditions but are less well-clustered for mixed conditions.

5. Conclusions

Clustering of \bar{B}_n for Durban, South Africa, produced four classes with diurnal patterns as follows: sunny all day (Class A), cloudy all day (Class B), sunny morning and cloudy afternoon (Class C) and cloudy morning and sunny afternoon (Class D). These results provide a classification of beam irradiance profiles for Durban, and a novel approach to day-ahead forecasting using classification of cloud cover predictions, in particular by clustering. Day-ahead forecasts have value in predicting the general daily profile and are useful for constraining models for multi-hour predictions on a particular day. Further work that will be useful to better characterise irradiance patterns and produce day-ahead forecasts includes use of diffuse irradiance and sub-hourly variability of beam irradiance.

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